FABER POLYNOMIAL COEFFICIENTS FOR GENERALIZED BI–SUBORDINATE FUNCTIONS OF COMPLEX ORDER

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Abstract. In this paper, we obtain the upper bounds for the n-th ($n \geqslant 3$) coefficients for generalized bi-subordinate functions of complex order by using Faber polynomial expansions. The results, which are presented in this paper, would generalize those in related works of several earlier authors.

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